The Challenge	MSOS	Control Operators	Conclusion	Extra Slides

A Modular Structural Operational Semantics for Delimited Continuations

Neil Sculthorpe, Paolo Torrini and Peter D. Mosses

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The Challenge

"While the use of labels gives MSOS the ability to modularly deal with some forms of control, such as abrupt termination, at our knowledge it still cannot support the definition of arbitrarily complex control-intensive features such call/cc."

The Journal of Logic and Algebraic Programming 79 (2010) 397-434



An overview of the K semantic framework

Grigore Roșu*, Traian Florin Șerbănuță

Department of Computer Science, University of Minois at Urbana-Chempeign, 201 N Goodwin, Urbane, & 61801, USA

ITICLE INFO	ABSTRACT
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1. Introduction

This paper is a gendle introduction to K, a reventing-based semantic definitional framework. K was introduced by the first author in the leven mores of a programming language concers at the University of Illinois at University (III) (III) for Fall 2000 [14], as a means to define executable concurrent languages in rewriting logic using Maude [7]. Since 2003, K has research initiatives, more formig descriptions of K only for Bound (113 Sal).

The introduction and development of K was largely motivated by the observation that after more than 40 years of systematic research in programming language semantics, the following important (multi-)question remains largely open to the working programming language designer, but also to the entire research community:

Is there any language definitional framework which, at the same time,

- Cines a unified approach to define not only impagate but also impagate-related abstractions, such as type checkers, type inferences, abstract interpreters, safety policy or domain specific heckers, set: 7 the current state-of-the art is that language designess use different approaches or styles to define different aspects of a language, sometimes even to define different components of the same aspect.
- Can define arbitrarily complex language features, including, obviously, all those found in existing languages, capturing also their intended computational granularity? For example, features like call-with-current-continuation and true concurrency are hard or impossible to define in many existing frameworks.

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Neil Sculthorpe, Paolo Torrini & Peter D. Mosses

A Modular SOS for Delimited Continuations

The Challenge

"While the use of labels gives MSOS the ability to modularly deal with some forms of control, such as abrupt termination, at our knowledge it still cannot support the definition of arbitrarily complex control-intensive features such call/cc."

Yes it can!

The Journal of Logic and Algebraic Programming 79 (2010) 207-414



An overview of the K semantic framework

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This paper gives an overview of the K framework: what it is, how it can be used, and where it has been used as fast. It also proposes and discusses the K definition of CUALLENCE, a programming language that aims to challenge and expose the limitations of existing semantife frameworks.

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This paper is a genthe introduction to K a reverting-based eemantic definitional framework. Hwaci introduced by the first author in the lecture notes of a programming language course at the University of Illinois at Uthana-Champaign (UUC) in Sil 2003 [34], as a means to define executable concurrent languages in reverting logic using Maude [7]. Since 2003, K has been used continuously in teaching programming languages at UUC, in seminars in Spain and Romania, as well as in several research instative. A more formal description of K can be found in [35,36].

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A Modular SOS for Delimited Continuations

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(And control/prompt, and shift/reset.)

The Journal of Logic and Algebraic Programming 79 (2000) 297-434



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A Modular SOS for Delimited Continuations

The Challenge	MSOS	Control Operators	Conclusion	Extra Slides
This Talk				

- Overview and motivate MSOS
- MSOS specifications of control and prompt

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The Challenge	MSOS	Control Operators	Conclusion	Extra Slides
This Talk				

- Overview and motivate MSOS
- MSOS specifications of *control* and *prompt*
- Specifications of *shift* and *call/cc* in terms of *control* and *prompt*

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Modular Structural Operational Semantics (MSOS)

- A *modular* variant of Plotkin's SOS framework. $\frac{\rho_2 \vdash Y \xrightarrow{s_2} Y'}{\rho_1 \vdash X \xrightarrow{s_1} X'}$
- Benefit: rules need not mention unused auxiliary entities.
- We use a flavour of MSOS called *Implicitly Modular SOS* (I-MSOS):
 - unmentioned entities are propagated between premise and conclusion;
 - when there is no premise, unmentioned signals have a default value.
- This talk will use *small-step* transition rules.

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I-MSOS Specification of Lambda Calculus

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I-MSOS Specification of Lambda Calculus

$$\frac{\rho(I) = V}{\operatorname{env} \rho \vdash \mathbf{bv}(I) \to V}$$



MSOS

Control Operators

Conclusion

Extra Slides

I-MSOS Specification of Lambda Calculus

$$E ::= V$$

$$| bv(I)$$

$$| ambda(I, E)$$

$$| apply(E, E)$$

$$| \dots$$

$$V ::= closure(\rho, I, E)$$

$$| \dots$$

$$\frac{\rho(I) = V}{\operatorname{env} \rho \vdash \mathbf{bv}(I) \to V}$$

env $\rho \vdash \text{lambda}(I, E) \rightarrow \text{closure}(\rho, I, E)$

MSOS

Control Operators

Conclusion

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Extra Slides

I-MSOS Specification of Lambda Calculus

$$E ::= V$$

$$| bv(I)$$

$$| ambda(I, E)$$

$$| apply(E, E)$$

$$| \dots$$

$$V ::= closure(\rho, I, E)$$

$$| \dots$$

$$\frac{\rho(I) = V}{\operatorname{env} \rho \vdash \mathbf{bv}(I) \to V}$$

env $\rho \vdash \text{lambda}(I, E) \rightarrow \text{closure}(\rho, I, E)$

$$\frac{\operatorname{val}(V) \quad \operatorname{env} (\{I \mapsto V\}/\rho) \vdash E \to E'}{\operatorname{env} _\vdash \operatorname{apply}(\operatorname{closure}(\rho, I, E), V) \to \operatorname{apply}(\operatorname{closure}(\rho, I, E'), V)}$$

$$\frac{\operatorname{val}(V_1) \quad \operatorname{val}(V_2)}{\operatorname{env} \rho \vdash \operatorname{apply}(\operatorname{closure}(\rho, I, V_1), V_2) \to V_1}$$

he Challenge N	ISOS	Control Operators	Conclusion
-MSOS Specif	ication	of Lambda Ca	alculus
E)/		$\frac{\rho(I) = V}{\operatorname{env} \rho \vdash \operatorname{bv}(I) \to V}$	7
L V bv(I) lambda(I, E)	env $\rho \vdash$ lambda (I ,	$(E,E) \rightarrow \text{closure}(ho,I,E)$
$V ::= closure(\rho, I, I)$	E)	apply(E ₁ ,	$\frac{E_1 \to E_1'}{E_2) \to apply(E_1', E_2)}$
		$\frac{val(V)}{apply(V)}$	$\frac{E \to E'}{E) \to \operatorname{apply}(V, E')}$
env _ ⊢ app	val(V) ly(closure	$\operatorname{env}\left(\{I\mapsto V\}/\mu\right)$	$p) \vdash E \rightarrow E'$ $ply(closure(\rho, I, E'), V)$
-	ар	$val(V_1)$ $val(V)$ $ply(closure(ho, I, V_2)$	V_2) 1), V_2) $ ightarrow$ V_1

Extra Slides

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$$E, H ::= \operatorname{throw}(E) \\ | \operatorname{catch}(E, H) \\ | \operatorname{stuck} \\ | \cdots \\ Val(V) \\ \hline \operatorname{throw}(V) \xrightarrow{\operatorname{exc some}(V)} \operatorname{stuck} \\ \hline$$

$$\frac{E \xrightarrow{\text{exc none}} E'}{\text{catch}(E, H) \xrightarrow{\text{exc none}} \text{catch}(E', H)}$$

$$\frac{E \xrightarrow{\text{exc some}(V)} E'}{\text{catch}(E, H) \xrightarrow{\text{exc none}} \text{apply}(H, V)}$$

$$\frac{\text{val}(V)}{\text{catch}(V, H) \xrightarrow{\text{exc none}} V}$$

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$$\begin{bmatrix} E, H ::= \text{throw}(E) \\ | & \text{catch}(E, H) \\ | & \text{stuck} \\ | & \cdots \end{bmatrix} \xrightarrow{E \longrightarrow E'} \\ \hline \text{throw}(E) \longrightarrow \text{throw}(E') \\ \hline \text{val}(V) \\ \hline \text{throw}(V) \xrightarrow{\text{exc some}(V)} \text{stuck} \\ \hline \end{bmatrix}$$

$$\frac{E \xrightarrow{\text{exc none}} E'}{\text{catch}(E, H) \xrightarrow{\text{exc none}} \text{catch}(E', H)} \frac{E \xrightarrow{\text{exc some}(V)} E'}{\text{catch}(E, H) \xrightarrow{\text{exc none}} \text{apply}(H, V)} \frac{\text{val}(V)}{\text{catch}(V, H) \longrightarrow V}$$

e

SOS Specification of Lambda Calculus with Exceptions

$$\frac{\rho(I) = V}{\text{env } \rho \vdash \mathbf{bv}(I) \xrightarrow{\text{exc none}} V}$$

env $\rho \vdash \text{lambda}(I, E) \xrightarrow{\text{exc none}} \text{closure}(\rho, I, E)$

$$\begin{array}{c} \underbrace{ \operatorname{env} \rho \vdash E_{1} \xrightarrow{\operatorname{exc} X} E_{1}' \\ \hline \\ \hline \operatorname{env} \rho \vdash \operatorname{apply}(E_{1}, E_{2}) \xrightarrow{\operatorname{exc} X} \operatorname{apply}(E_{1}', E_{2}) \\ \hline \\ \underbrace{ \operatorname{val}(V) \qquad \operatorname{env} \rho \vdash E \xrightarrow{\operatorname{exc} X} E' \\ \hline \\ \operatorname{env} \rho \vdash \operatorname{apply}(V, E) \xrightarrow{\operatorname{exc} X} \operatorname{apply}(V, E') \\ \hline \\ \underbrace{ \operatorname{val}(V) \qquad \operatorname{env} \left(\{I \mapsto V\} / \rho \right) \vdash E \xrightarrow{\operatorname{exc} X} E' \\ \hline \\ \operatorname{env} _ \vdash \operatorname{apply}(\operatorname{closure}(\rho, I, E), V) \xrightarrow{\operatorname{exc} X} \\ \operatorname{apply}(\operatorname{closure}(\rho, I, E'), V) \\ \hline \\ \underbrace{ \operatorname{val}(V_{1}) \qquad \operatorname{val}(V_{2}) \\ \hline \\ \operatorname{env} \rho \vdash \operatorname{apply}(\operatorname{closure}(\rho, I, V_{1}), V_{2}) \xrightarrow{\operatorname{exc} \operatorname{none}} V_{1} \end{array}$$

$$\frac{\operatorname{env} \rho \vdash E \xrightarrow{\operatorname{exc} X} E'}{\operatorname{env} \rho \vdash \operatorname{throw}(E) \xrightarrow{\operatorname{exc} X} \operatorname{throw}(E')}$$

$$\frac{\operatorname{val}(V)}{\operatorname{env} \rho \vdash \operatorname{throw}(V) \xrightarrow{\operatorname{exc} \operatorname{some}(V)} \operatorname{stuck}}$$

$$\frac{\operatorname{env} \rho \vdash E \xrightarrow{\operatorname{exc} \operatorname{none}} E'}{\operatorname{env} \rho \vdash \operatorname{catch}(E, H) \xrightarrow{\operatorname{exc} \operatorname{none}} \operatorname{catch}(E', H)}$$

$$\begin{array}{c} \underbrace{ \mbox{env} \ \rho \vdash E \xrightarrow{\mbox{exc none}} E' \\ \hline env \ \rho \vdash \mbox{catch}(E, H) \xrightarrow{\mbox{exc none}} apply(H, V) \\ \hline \hline \underbrace{ \ val(V) \\ \hline env \ \rho \vdash \mbox{catch}(V, H) \xrightarrow{\mbox{exc none}} V \end{array}$$

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Neil Sculthorpe, Paolo Torrini & Peter D. Mosses A Modular SOS for Delimited Continuations

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I-MSOS Specification of Lambda Calculus with Exceptions

$$\begin{array}{c} \rho(l) = V \\ \hline env \ \rho \vdash bv(l) \longrightarrow V \\ env \ \rho \vdash bv(l) \longrightarrow V \\ env \ \rho \vdash lambda(l, E) \longrightarrow closure(\rho, l, E) \\ \hline E_1 \longrightarrow E'_1 \\ \hline apply(E_1, E_2) \longrightarrow apply(E'_1, E_2) \\ \hline Val(V) \qquad E \longrightarrow E' \\ \hline apply(V, E) \longrightarrow apply(V, E') \\ \hline Val(V) \qquad env \ (\{l \mapsto V\}/\rho) \vdash E \longrightarrow E' \\ env _\vdash apply(closure(\rho, l, E), V) \longrightarrow \\ \hline apply(closure(\rho, l, E), V) \longrightarrow \\ apply(closure(\rho, l, K), V_2) \longrightarrow V_1 \\ \hline \end{array}$$



• We formulate *control* as a unary operator that takes a higher-order function as its argument:

$$1 + prompt(2 * control(\lambda k. k(k 7))) \quad \rightsquigarrow \quad 29$$

• In our notation:

plus(1, prompt(times(2, control(lambda(K, apply(bv(K), apply(bv(K), 7)))))))

Key ideas:

- We *don't* maintain an explicit representation of the current continuation.
- We *construct* the continuation from the program term when needed.
- Use *signals* to communicate between control operators and delimiters:
 - **control** emits a signal when executed;
 - prompt catches that signal and handles it.

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$$E \xrightarrow{\text{control none}} E'$$

$$prompt(E) \xrightarrow{\text{control none}} prompt(E')$$

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$$E ::= control(E) | prompt(E) | ...
$$E \rightarrow E' control(E) \rightarrow control(E') val(F) fresh-id(I) control(F) control some(F,I) bv(I)
$$E control rone E' prompt(E) control none prompt(E') E control some(F,I) E' K = lambda(I, E') prompt(E) control none prompt(apply(F, K)) val(V) prompt(V) \rightarrow V$$$$$$



The Challenge	MSOS	Control Operators	Conclusion	Extra Slides
The Meta-env	vironment			

- An auxiliary environment that doesn't interact with closures.
- Used here to achieve the same effect as substitution.

$$ho(I) = V$$

meta-env $ho dash$ meta-bv $(I)
ightarrow V$

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$$\begin{array}{c} \operatorname{meta-env} \rho \vdash E_1 \to E_1' \\ \hline \operatorname{meta-env} \rho \vdash \operatorname{meta-let-in}(I, E_1, E_2) \to \operatorname{meta-let-in}(I, E_1', E_2) \\ \hline \operatorname{wal}(V) \quad \operatorname{meta-env} (\{I \mapsto V\}/\rho) \vdash E \to E' \\ \hline \operatorname{meta-env} \rho \vdash \operatorname{meta-let-in}(I, V, E) \to \operatorname{meta-let-in}(I, V, E') \\ \hline \operatorname{wal}(V_1) \quad \operatorname{val}(V_2) \\ \hline \operatorname{meta-env} \rho \vdash \operatorname{meta-let-in}(I, V_1, V_2) \to V_2 \end{array}$$

The Challenge	MSOS	Control Operators	Conclusion	Extra Slides
Conclusion				

- MSOS allows programming constructs to be specified *independently*.
- Contrary to popular belief, specifying control operators in MSOS is fairly straightforward.
- In the paper we have also specified *call/cc*, *shift* and *reset*.
- Specifications tested on 70 test programs (including Mondo Bizarro!), using our I-MSOS interpreter.
- Test suite available online: http://www.plancomps.org/woc2016



• i.e. $shift(f) = control(\lambda k. f(\lambda x. reset(k x)))$

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I-MSOS Specification of *abort* and *call/cc*

$$\frac{E \to E'}{\text{abort}(E) \to \text{abort}(E')}$$

 $\frac{\operatorname{val}(V) \quad \operatorname{fresh-id}(I)}{\operatorname{abort}(V) \to \operatorname{control}(\operatorname{lambda}(I,V))}$

MSOS

Control Operators

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Extra Slides

I-MSOS Specification of *abort* and *call/cc*

$$\frac{E \to E'}{\operatorname{abort}(E) \to \operatorname{abort}(E')}$$

 $\frac{\operatorname{val}(V) \quad \operatorname{fresh-id}(I)}{\operatorname{abort}(V) \to \operatorname{control}(\operatorname{lambda}(I,V))}$

$$\frac{E \to E'}{\operatorname{callcc}(E) \to \operatorname{callcc}(E')}$$

$$\frac{\operatorname{val}(F) \quad \operatorname{fresh-id}(K) \quad \operatorname{fresh-id}(X)}{\operatorname{callcc}(F) \to}$$

control(lambda(K, apply(bv(K), apply(F, lambda(X, abort(apply(bv(K), bv(X))))))))

- i.e. $callcc(f) = control(\lambda k. k (f (\lambda x. abort(k x))))$
- N.B. To simulate an undelimited *call/cc*, the program should contain only a single top-level delimiter.

Eugene Kohlbecker's Mondo Bizarro

let mondo_bizarro () = let
$$k$$
 = callcc(function $c \rightarrow c$)
in print 1;
callcc(k);
print 2;
callcc(k);
print 3;;

prompt(mondo_bizarro()) ;;

Output: [1;1;2;1;3]

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